acid is in sufficient excess over sarin so that its concentration remains substantially constant during the course of reaction. Under these conditions, the reaction rate, $k_{\text {obs }}$, cant be calculated from equation 7 which is derived from equations 5 and $6 .{ }^{16}$

$$
\begin{equation*}
k_{\text {obs }}=\frac{G_{\mathrm{B}}\left[\mathrm{HA}_{\text {rot }}\right] K_{\mathrm{A}}}{\left[\mathrm{H}^{+}\right]+K_{\mathrm{A}}}\left(\frac{K_{\mathrm{w}}}{K_{\mathrm{A}}}\right)^{\beta} \mathrm{sec}^{-1} \tag{7}
\end{equation*}
$$

Substituting numerical values for $G_{\mathrm{B}}$ and $\beta$ established above, we obtain

$$
\begin{equation*}
k_{\mathrm{obs}}=\frac{3.5 \times 10^{-9}\left[\mathrm{HA}_{\mathrm{Tot}}\right] K_{\mathrm{A}^{0.20}}}{\left[\mathrm{H}^{+}\right]+K_{\mathrm{A}}} \mathrm{sec} .^{-1} \tag{7a}
\end{equation*}
$$

As an example, we have plotted in Fig. 4 the quantitative relationship between reaction half-
(16) For derivation and discussion of these relationships, see J. Fpstein. D. E. Rosenblatt and M. Demek. This Journal, 78, 341 (1956), and G. M. Steinberg, R. Swidler and S. Seltzer. Science, 125, 336 (195\%). Similar relationships have been developed independently by A. L. Green. G. L. Sainsbury and M. Stansfield, private communicam tion.
time $\left(t_{1 / 2}=0.693 / k_{\text {obs }}\right)$ and hydroxanic acid $p K_{\mathrm{A}}$ at $\left[\mathrm{HA}_{\text {Tot }}\right]=10^{-3} M$, and at $p \mathrm{H} 7.6$, under the stipulated conditions.

The general relationship between $p K_{\mathrm{A}}$ and $p \mathrm{H}$ for maximum reaction rate at fixed $p \mathrm{H}$, equation 8 , can be derived from equation 7 by integration of the expression $\mathrm{d} k_{\mathrm{obs}} / \mathrm{d} \mathbb{K}_{\mathrm{A}}=0$. For the reaction

$$
\begin{equation*}
p K_{\mathrm{A}}-p \mathrm{H}=\log \frac{\beta}{1-\beta} \tag{8}
\end{equation*}
$$

under consideration in the present study, where the value of $\beta=0.80$, maximum rate will be obtained with the hydroxamic acid of $p K_{\mathrm{A}}=p \mathrm{H}+0.60$.

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Chemical Cevter, Md.

## [Contribution from the Department of Chemistry, University of Cincinnati]

# An Acidity Function for the Solvent System Consisting of 20 Vol. \% Ethanol and 80 Vol. \% Sulfuric Acid-Water Mixtures ${ }^{1}$ 

By Si-Jung Yeh and H. H. Jaffé<br>Received December 20, 1958

A series of 32 mono- and disubstituted derivatives of azobenzene was used to establish an $H_{0}$ scale in the solvent system $20 \%$ ethanol- $80 \%$ sulfuric acid-water mixture. $o$ - and $p$-nitroaniline were used to connect this scale to potentiometrically measured $p \mathrm{H}$ 's. The scale extends from dilute solution to 19 Nacid . The scale is of particular interest since the indicators used are structurally closely related, and the $\mathrm{B} / \mathrm{BH}^{+}$vs. acid concentration curves for the various indicators are almost exactly parallel in the overlap regions. The scale is compared with the $H_{0}$ scale in aqueous sulfuric acid.

The $H_{0}$ function originally introduced by Hammet and co-workers ${ }^{2}$ is a tremendously useful acidity scale for the measurement of base strengths of weak, uncharged bases in aqueous acids, because it provides a quantitative measure of the ability of the aqueous solution under consideration to transfer a proton to the uncharged base. The $I_{0}$ functions for aqueous solutions of various strong acids have been established by the use of series of different indicators such as the derivatives of aromatic amines. ${ }^{3}$ A basic requirement for the validity of an acidity function is that the plot of $\log$ $\left(\mathrm{B}^{\prime} / \mathrm{BH}^{-}\right)$vs. acid concentration be parallel for all indicators used in the regions of overlapping acid concentrations in which measurement of $\log$ ( $\mathrm{B} /$ $\mathrm{BH}^{+}$) is experimentally possible. ${ }^{3}$ This condition has rarely been met in the past. It lias been suggested that the use of structurally closely related indicators would greatly aid in achieving this ideal. ${ }^{., 3}$

Many weak organic bases are insufficiently soluble in dilute aqueous acid for convenient measurements of the $p K$ by a spectrophotometric method, but addition of a snnall amount of an organic solvent, e.g., ethanol, permits such measurements. Although the concept of the $I_{0}$ function
(1) This work was supported by a Bonita Ceho Memorial Grant for Cancer Research from the American Cancer Society. This support is gratefully acknowledged.
(2) L. P. Hammett and A. J. Deyrup. This Journal. 64, 2721 (1932).
(3) M. A. Paul and F. A. Long, Chem. Reos., 57, 1 (1957).
can be extended to mixed solvent systems, the addition of a solvent with low dielectric constant to the aqueous acid also raises a problem as to the validity of the $I_{0}$ function in such mixed solvent systems.

The $H_{0}$ function for solutions of hydrochloric acid in ethanol has been studied by Bratude ${ }^{4}$ up to $1 M$ acid concentration using a single indicator, $p$ nitroaniline. Braude and Stern ${ }^{5}$ have extended this study to a mixed solvent system containing varying proportions of ethanol at fixed hydrochloric acid concentrations of $0.1 M$ and $1 M$, and have reported that, with increasing ethanol concentration, $H_{0}$ goes through a minimum at equimolar proportion of the two solvent. Grunwald and co-workers ${ }^{6}$ have measured the $p K^{\prime}$ 's of various uncharged bases in ethanol and water mixtures by a potentiometric method, and found that the $p K^{\prime}$ 's in the mixed solvents are significantly different from the values in pure water; c.g. the $p K$ of aniline goes from 4.64 in pure water to 4.16 in 35 wt. \% ethanol, passes through a minimum of 3.75 at $80 \mathrm{wt} . \%$ ethanol and increases to 5.70 in pure ethanol. These data demonstrate that the $p K$ values are dependent on the solvent system and that for the measurenient of the $p K$ of a weak un-

[^0] (195:).

Table I
Physical Properties and Analyses of Azo Compounds


| x |  |  |  |  |  |  |  | Crude <br> yield. |  |  |  | $\lambda$, m | ${ }_{\text {eB }}$ | ¢ $\mathrm{BH}^{+}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\overparen{\text { Calcd. }}$ | Found | $\frac{-\mathrm{Anal}}{\mathrm{Calcd} .}$ | Found <br> (a) | Calcd. $\mathrm{Y}=m-1$ | Found |  | $\widehat{\lambda, \mathrm{m} \mu}$ | ${ }_{\epsilon B}^{\lambda_{B}{ }^{\text {p }} \text {, }}$ | $\underset{\text { e }{ }^{\text {H }}+}{ }$ |  |  |  |
| p- $\mathrm{OC}_{2} \mathrm{H}_{5}$ | 101-102 ${ }^{\text {c }}$ | 61.98 | 62.36 | 4.82 | 4.75 | 15.55 | 15.33 | 89 | 352 | 1.99 | 0.220 | 464 | 0.305 | 4.82 |
| p- $\mathrm{OCH}_{3}$ | 113-114 | 60.70 | 60.95 | 4.31 | 4.31 | 16.33 | 16.49 | 90 | 354 | 2.27 | 228 | 468 | . 193 | 4.64 |
| $p-\mathrm{CH}_{3}$ | 117-118 | 64.72 | 64.85 | 4.54 | 4.40 | 17.42 | 17.51 | 70 | 330 | 2.14 | . 363 | 430 | . 118 | 3.21 |
| $m \cdot \mathrm{CH}_{3}$ | 73-74 | 64.72 | 64.68 | 4.54 | 4.37 | 17.42 | 17.49 | 80 | 318 | 1.84 | 280 | 418 | . 020 | 2.63 |
| $p-\mathrm{Br}^{\text {d }}$ | 118-119 | 47.08 | 47.23 | 2.63 | 2.47 | 13.73 | 13.58 | 81 | 328 | 2.32 | . 405 | 440 | . 100 | 3.48 |
| $m-\mathrm{Br}^{\circ}$ | 107-108 | 47.08 | 47.45 | 2.63 | 2.53 | 13.73 | 13.81 | 91 | 312 | 1.99 | . 457 | 412 | . 061 | 2.46 |
| $p \cdot \mathrm{COCH}_{4}$ | 114-115 | 62.45 | 62.47 | 4.12 | 4.25 | 15.61 | 15.77 | 85 | 320 | 2.60 | . 507 | 416 | . 048 | 3.03 |
| $m$ - $\mathrm{COCH}_{3}$ | 105-106 | 62.45 | 62.17 | 4.12 | 4.21 | 15.61 | 15.87 | 85 | 316 | 1.92 | . 552 | 410 | . 034 | 2.56 |
| $p$-CN | 134-135 | 61.90 | 62.07 | 3.20 | 3.23 | 22.21 | 22.06 | 90 | 318 | 2.50 | . 600 | 410 | . 043 | 2.94 |
| $m-\mathrm{NO}_{2}{ }^{\text {f }}$ | 151-152 |  |  |  | (b) | $\mathrm{Y}=p-\mathrm{O}$ |  |  | 268 | 2.34 | 1.46 | 400 | . 035 | 2.58 |
| $p-\mathrm{OCH}_{3}$ | 143-144 ${ }^{\text {a }}$ |  |  |  |  | 12.28 | 12.22 | 92 | 360 | 2.50 | 0.250 | 490 | 0.045 | 4.09 |
| $p$ - $\mathrm{CH}_{3}$ | 153-153. $5^{\text {h }}$ |  |  |  |  | 13.33 | 13.20 | 90 | 350 | 2.48 | 270 | 470 | . 140 | 4.10 |
| $\mathrm{H}^{\text {i }}$ | $155-156^{i}$ |  |  |  |  |  |  | 91 | 346 | 2.21 | . 250 | 460 | 110 | 3.99 |
| $p-\mathrm{Br}$ | 160-161 ${ }^{\text {i }}$ |  |  |  |  | 10.11 | 10.21 | 89 | 356 | 2.61 | . 275 | 480 | . 085 | 4.4 |
| $m-\mathrm{Br}$ | $142-143^{k}$ |  |  |  |  | 10.11 | 9.91 | 76 | 356 | 2.29 | . 280 | 460 | . 135 | 4.15 |
| $p-\mathrm{COCH}_{3}$ | 198-199 | 69.98 | 70.33 | 5.04 | 5.08 | 11.66 | 11.47 | 90 | 360 | 2.58 | . 310 | 480 | . 210 | 4.75 |
|  |  | (c) $\mathrm{Y}=p-\mathrm{OCH}_{3}$ |  |  |  |  |  |  |  |  |  |  |  |  |
| $p-\mathrm{OCH}_{3}$ | 165-166 ${ }^{\text {l }}$ |  |  |  |  | 11.66 | 11.57 | 70 | 360 | 2.57 | 0.250 | 490 | 0.230 | 4.45 |
| $p-\mathrm{CH}_{3}$ | 111-112 ${ }^{\text {m }}$ |  |  |  |  | 12.18 | 12.30 | 72 | 350 | 2.46 | . 320 | 470 | . 240 | 4.21 |
| $p-\mathrm{Br}^{n}$ | 148-149 | 53.62 | 53.85 | 3.81 | 3.75 | 9.62 | 9.74 | 75 | 350 | 2.63 | . 490 | 480 | . 110 | 4.72 |
| $m-\mathrm{Br}^{\circ}$ | 62-63 | 53.62 | 53.74 | 3.81 | 3.79 | 9.62 | 9.49 | 60 | 250 | 2.20 | . 290 | 470 | 200 | 4.48 |

${ }^{a}$ Uncorrected. ${ }^{b}$ Microanalyses were performed by A. Bernhardt, Mühlheim (Ruhr), Germany. ${ }^{6}$ M.p. $96^{\circ}$; E. Baly, W. Tuck and E. Marsden, J. Chem. Soc., 97,1501 (1910). ${ }^{d} \mathrm{Br}$ calcd. $2 \overline{5} .79$, found $25.88 .{ }^{\text {e }} \mathrm{Br}$ calcd. 25.79 , found $2 \overline{5} .88$. $f$ This compound was kindly provided by Prof. E. Malmberg, Ohio State University. ${ }^{\circ}$ M.p. $142^{\circ}$; K. Kraus, Ber., 32, 124 (1899). ${ }^{h}$ M.p. $151^{\circ}$; E. Grandmonugin and H. Freimann, J. prakt. Chem., [2] 78, 392 (1909). ${ }^{i}$ Since this is a well known compound, no analysis was performed; m.p. $156^{\circ}$; K. H. Engel, This Journal, 51, 2989 (1929). ${ }^{i}$ M.p. $162^{\circ}$; J. J. Fox and J. T. Hewitt, J. Chem. Soc., $93,340(1908){ }^{k}$ M.p. $139-140^{\circ} ;$ P. Jacobson, G. Franz and K. Zaar, Ber., 36, 3867 (1903). $i$ M.p. $165^{\circ} ; \mathrm{D}$. Vorländer, ibid., $40,1422(1907) .{ }^{m}$ M.p. $110-111^{\circ} ; ~ H$. Wieland, ibid., 48,1107 (1915). ${ }^{n}$ Br calcd. 27.45 , found 27.67 . o Br calcd. 27.45, found 27.83. $p$ The wave lengths given are not necessarily absorption maxima although they are usually quite close to them.
charged base in mixed solvent systems the original $H_{0}$ function cannot be used.

In connection with the study of the effect of substituents on the basicities of monosubstituted azobenzenes, Jaffé and Gardner ${ }^{7}$ have established, based on $p$-nitroazobenzene as an arbitrary standard, an acidity scale for the solvent system consisting of 20 vol. $\%$ EtOH and 80 vol. $\% \mathrm{H}_{2} \mathrm{SO}_{4}-$ $\mathrm{H}_{2} \mathrm{O}$ mixtures. Their acidity scale covered acidity ranges from 20 to $55 \mathrm{wt} . \% \mathrm{H}_{2} \mathrm{SO}_{4}$. It appeared desirable to connect their acidity function to the $p \mathrm{H}$ scale and to extend it to higher acidity ranges. For this purpose we have prepared three series of disubstituted azobenzenes and measured the concentration ratios, $c_{\mathrm{B}} / c_{\mathrm{BH}}+$ in this particular solvent system by the spectrophotometric method. ${ }^{8}$ Here $c_{\mathrm{B}}$ and $c_{\mathrm{BH}}+$ are, respectively, the concentrations of the free base and of the conjugate acid of the substituted azobenzenes. Hammett's method was used to establish the $H_{0}$ scale.

## Experimental

Compounds: Substituted Anilines.-Commercially available $p$-nitroaniline and $o$-nitroaniline were recrystallized twice from water and $95 \%$ ethanol, respectively; $p$-nitroaniline (m.p. 148-148.5 ${ }^{\circ}$; o-nitroaniline, m.p. $72-73^{\circ}$;
(7) H. H. Jaffé and R. W. Gardner, This Journal. 80, 319 (1958), (8) L. A. Flexser, L. P. Hammett and A. Dingwall, ibid., 87, 2103 (1935).
reported ${ }^{9}$ in the literature are 147.5 and $71.5^{\circ}$, respectively). Disubstituted Azobenzenes.-The $m$-(arylazo)-nitrobenzenes were prepared by condensation of appropriately substituted anilines with $m$-nitrosonitrobenzene in glacial acetic acid. ${ }^{10} m$-Nitrosonitrobenzene was obtained by the oxidation of $m$-nitroaniline with Caro acid. ${ }^{11}$

The $p$-(arylazo)-phenols were prepared by coupling phenol in alkaline solution with diazonium chlorides obtained by diazotization of the appropriately substituted anilines. ${ }^{12}$

The $p$-(arylazo)-phenols were methylated with dimethyl sulfate in alkaline solution to give $p$-(arylazo)-anisoles. ${ }^{13}$

All azo-compounds were recrystallized repeatedly from ethanol until constant melting points were obtained. Elemental analysis confirmed the purities of these compounds. The physical properties and analyses of all azo-compounds are summarized in Table I.

Determination of the Concentration Ratios $c_{\mathrm{B}} / c_{\mathrm{BH}}{ }^{+}$by the Spectrophotometric Method: (a) Preparation of Solu-tions.-A stock solution of azo-compound $\left(1 \times 10^{-4} M\right)$ was prepared in $95 \%$ ethanol. Aliquots ( 10 ml .) of the stock solution were pipetted into a series of 50 ml . volumetric flasks, placed in a thermostat at $25.0 \pm 0.1^{\circ}$, and then diluted to the mark with aqueous sulfuric acid solutions of appropriate concentration. In this way a series of solutions was obtained in which the concentration of azo compound and the content of ethanol were identical but which had varying acid concentration.

[^1](b) Determination of Acidity of the Solutions.-When the sulfuric acid concentration was low enough to permit $p \mathrm{H}$ measurements, the acidity of the solution under investigation was determined by a Beckman model G pH meter. The $p \mathrm{H}$ scale of the instrument was calibrated with standard buffer solution before use. For the solutions of higher acid concentration, the acidity was determined by a calibration chart of density vs. sulfuric acid content. ${ }^{7}$
(c) Measurements of Concentration Ratios $c_{\mathrm{B}} / c_{\mathrm{BH}^{+}}$.The concentration ratios $c_{\mathrm{B}} / c_{\mathrm{BH}^{+}}$of the azi)-compounds were measured by use of a Beckman DU quartz spectrophotometer using l-cm. silica cells. The cell connpartnent
of 20 vol . To ethanol and $80 \mathrm{vol} . \% \mathrm{H}_{2} \mathrm{SO}_{4}-\mathrm{H}_{2} \mathrm{O}$ mixture is given by
\[

$$
\begin{equation*}
p K=-\log \frac{c_{\mathrm{BH}}}{c_{\mathrm{BH}^{+}}}-\log \frac{a_{\mathrm{H}}+f_{\mathrm{B}}}{f_{\mathrm{BH}^{+}}} \tag{1}
\end{equation*}
$$

\]

When the $\mathrm{H}_{2} \mathrm{SO}_{4}$ content is low enough for measurement of the $p H$ of the solution, the $p K$ of the base in this particular system can be obtained directly from eq. 1. This technique was used to set the standard of the $H_{0}$ function for this mixed solvent system. Since it was not possible to obtain disubstituted azobenzenes of strong enough basicity to


Fig. 1.-Plot of $\log \left(c_{\mathrm{B}} / c_{\mathrm{BH}}{ }^{+}\right)$es. $\mathrm{H}_{2} \mathrm{SO}_{4}$ concentration $\left.\mathrm{f}_{1}\right)$ sume of the indicators used: a, $p$ - $(m$-bromophenylazo)-anisole; b, $p$-( $p$-nitrophenylazı) -anisole; $c, m$-phenylazotolnene: $d$, azobenzene; e, $p$-bromoazobenzene; f, m-bromoazobenzene: g, $m$-( $m$-nitrophenylazn)-toluene.
was regulated at $25.00 \pm 0.02^{\circ}$ by a thermospacer assembly. When the solubility of the azo-compound is solow that $10-\mathrm{cm}$. cells must be used to obtain suitable absorbance, the measurement was carried out at room temperature of $25.0 \pm 0.5^{\circ}$. The concentration ratios $c_{\mathrm{B}} / c_{\mathrm{BH}^{+}}$were calculated by the method described elsewhere. ${ }^{7}$

Procedure for Establishing $H_{0}$ Function for the Solvent System Consisting of 20 Vol . $/ 7 \mathrm{EtOH}$ and $80 \mathrm{Vol} . \%$ $\mathrm{H}_{2} \mathrm{SO}_{4}-\mathrm{H}_{2} \mathrm{O}$ Mixtures.-In order to connect Jaffé and Gardner's $H_{0}{ }^{\prime}$ scale to the $p \mathrm{H}$ scale, it is necessary to use the concentration ratios $c_{\mathrm{B}} / c_{\mathrm{BH}^{+}}$data for the monosubstituted compounds were taken from the work of Gardner. ${ }^{14}$

The $p K$ of a weak base, B , in the solvent system consisting

permit the measurement of $c_{\mathrm{B}} / \mathcal{C B H}^{+}$at sufficiently low acidity, $p$ - and $o$-nitroaniline were used for this purpose.

As the $\mathrm{H}_{2} \mathrm{SO}_{4}$ content increases, one can no longer measure the $p \mathrm{H}$ of the solution and has to adopt the method of Hammett and Deyrup ${ }^{2}$ to extend the $H_{0}$.

$$
p K=-\log \frac{c_{\mathrm{B}}}{c_{\mathrm{BH}^{+}}}+H_{0}
$$

where

$$
H_{0} \equiv-\log \frac{a_{\mathrm{H}^{+}} f_{\mathrm{B}}}{f_{\mathrm{BH}^{+}}}
$$

For the mono- and disubstituted azobenzenes there is sufficient overlap of experimentally measurable concentration ratios $c_{\mathrm{B}} / c_{\mathrm{BH}^{+}}$(only concentration ratios in the range

Table II
The Procedure of the Extension of the $H_{0}$ Function

| N $\mathrm{H}_{2} \mathrm{SO}_{4}{ }^{\text {a }}$ | $\cdots{ }^{-}{ }_{0}{ }^{3}$ | $10 \mathrm{~g}(\mathrm{cb} / \mathrm{CBH}-)$ | $-\overline{-p K}_{t}^{c}{ }^{1}$ | $-\mathrm{H}_{0}{ }^{\text {d }}$ | $-p K_{\mathrm{f}}$ e | $\log _{( }\left(c_{B} / c_{B H}+\right)$ | $-p K_{t}{ }^{\text {c }}{ }^{\text {d }}$ | $-10_{0}{ }^{\text {i }}$ | $-p k_{6}{ }^{e}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) Indicator: $m$-brimmazabenzene, $\lambda_{1} 324 \mathrm{~m} \mu, \lambda_{z} 4.611 \mu$ |  |  |  |  |  |  |  |  |  |
| 11.12 | 3.28 | 1). 509 | ,3.79 |  | 3. 79 | 0. 531 | 3.81 |  | 3.81 |
| 11.51 | 3.45 | . 345 | 3.81 |  | 3.81 | . 407 | 3.86 | . | 3.86 |
| 11.82 | 3.59 | 267 | 3.86 |  | 3.86 | . 272 | 3.86 | . | ;3. 86 |
| 12.03 | 3.65 | 165 | 3.82 |  | 3.82 | . 134 | 3.78 |  | 3.78 |
| 12.44 |  | . 031 | $(3.83)^{\prime}$ | 3.80 | 3.86 | . 017 | (3.83) ${ }^{\text {t }}$ | 3.81 | 3.85 |
| 12.57 |  | - . 065 | $(3.83)^{\prime}$ | 3.90 | 3.82 | -. 106 | (3.83) ${ }^{\prime}$ | 3.94 | 3.78 |
| 12.97 |  | -. 211 | $(3.83)^{\prime}$ | 4.04 | 3.86 | -. 219 | $(3.83)^{f}$ | 4.05 | 3.85 |
| (1) Indicator: $m$-nitro-p'-methylazobenzene, ${ }^{8} \lambda_{1} 330 \mathrm{~m} \mu$, $\lambda_{2} 430 \mathrm{~m} \mu$ |  |  |  |  |  |  |  |  |  |
| 11.83 | 3.58 | 0.253 | 3.83 |  | 3.83 | 0.238 | 3.82 | . | 3.82 |
| 12.00 | 3.64 | 207 | 3.85 |  | 3.85 | . 164 | 3.80 | . | 3.80 |
| 12.15 | 3.70 | 127 | 3.83 |  | 3.83 | . 079 | 3.78 | . | 3.78 |
| 12.26 |  | 090) | $(3.82)^{\prime}$ | 3.73 | 3.85 | . 049 | (3.82) ${ }^{\text {f }}$ | 3.78 | 3.81 |
| 12.41 |  | . 021 | $(3.82)^{f}$ | 3.80 | 3.84 | -. 025 | $(3.82)^{f}$ | 3.84 | 3.79 |
| 12.52 |  | -. .056 | $(3.82)^{\prime}$ | 3.88 | 3.81 | -. 101 | $(3.82)^{t}$ | 3.92 | 3.76 |
| 12.85 |  | - .117 | $(3.82)^{\prime}$ | 3.94 | 3.89 | -. 155 | $(3.82)^{t}$ | 3.97 | ,3.85 |
| (c) Indicator: $p$-phenylazoacetophenone, $\lambda_{1} 330 \mathrm{~m} \mu, \lambda_{2} 420 \mathrm{~m} \mu$ |  |  |  |  |  |  |  |  |  |
| 11.32 | 3.37 | 0. $54 \%$ | 3.92 |  | 3.92 | 0.576 | 3.95 |  | 3.95 |
| 12.04 | 3.60 | . 322 | 3.92 |  | 3.92 | . 346 | 3.95 | $\ldots$ | 3. 35 |
| 12.27 | 3.76 | . 208 | 3.97 |  | 3.97 | . 235 | 4.00 | $\ldots$ | 4.00 |
| 12.58 | 3.89 | . 097 | 3.99 |  | 3.99 | . 121 | 4.01 |  | 4.01 |
| 12.86 | 4.01 | . 013 | 4.02 |  | 4.02 | . 040 | 4.05 |  | 4.05 |
| 13.17 |  | -. 138 | $(3.99)^{\prime}$ | 4.13 | 3.99 | -. 106 | $(3.99)^{i}$ | 4.10 | 4.02 |
| 13.34 |  | . 224 | $(3.99)^{\prime}$ | 4.21 | 3.98 | . 204 | $(3.99)^{i}$ | 4.19 | 4.00 |

${ }^{a}$ Determined from the density. ${ }^{b}$ As obtained from earlier compounds in the series. ${ }^{c}$ The "temporary" $p K$. ( $c f$. text), ${ }^{d}$ Calculated from this compound. EThe final value obtained from the smoothed $H_{0}$ function. f Average of the "temporary" $p K$ 's of this compound. "Since the $p K$ for this compound is essentially the same as for the previous one, these data give a duplicate of the extension of $H_{0}$.
0.2 to 5 were used) to apply this method. A typical example of such overlap is shown in Fig. 1 in which $\log \left[c_{B} /\right.$ $\left.c_{\mathrm{BH}^{+}}\right]$is plotted against the normality of $\mathrm{H}_{2} \mathrm{SO}_{4}$. A similar trend of overlap was observed in both lower acidity and higher acidity regions ( 1.5 N to $18 \mathrm{NH}_{2} \mathrm{SO}_{4}$ ). The concentration ratios of $p$-( $p$-methoxyphenylazo $)$-phenol, the strongest base in the series of disubstituted azobenzenes, overlap adequately with those of o-nitroaniline which served as the indicator to connect the $H_{0}$ function to the $p \mathrm{H}$ scale. The general procedure of stepwise extension of the $H_{0}$ function is illustrated by Table II. The $p K$ of $o$ nitroaniline was determined to be -0.336 in 20 vol. $\%$ ethanolic $\mathrm{H}_{2} \mathrm{SO}_{4}$ solution, and was used in conjunction with equation 2 to calculate the $H_{0}$ values for higher acid concentrations. $H_{0}$ values obtained here were used to calculate several values of a 'temporary $p K^{\prime \prime}$ of $p$-( $p$-methoxy-phenylazo)-phenol; these values were averaged and then used to extend the $H_{0}$ scale to higher $\mathrm{H}_{2} \mathrm{SO}_{4}$ concentration. This procedure was repeated for all substituted azobenzenes. All measurements of concentration ratios $c_{\mathrm{B}} / \mathrm{c}_{\mathrm{BH}^{+}}$were carried out at two wave lengths (one each near the absorption maxima of free base and of the conjugate acid, respectively), so that duplicate values of $c_{\mathrm{B}} / c_{\mathrm{BH}^{+}}$were available for each acid concentration. In addition, at least 3 or 4 independent pairs of the "temporary $p K$ values" were obtained for each compound and were found to be consistent with each other. After the $H_{0}$ function was extended to 19 $N \mathrm{H}_{2} \mathrm{SO}_{4}$, the curve was smoothed and the $p K$ of each compound was re-calculated using the $H_{0}$ values read from the smoothed curve. The $p K$ 's thus obtained did not differ from the 'temporary $p K$ '" by more than three hundredths of a $p K$ unit, and are summarized in Table IV.

## Results and Discussions

The $H_{0}$ values for the solvent system consisting of 20 vol. $\%$ ethanol and 80 vol. $\% \mathrm{H}_{2} \mathrm{SO}_{4}-\mathrm{H}_{2} \mathrm{O}$ mixtures are listed in Table III. A plot of $H_{0}$ vs. normality of $\mathrm{H}_{2} \mathrm{SO}_{4}$ is shown in Fig. 2 together with Hammett's $H_{0}$ function in aqueous sulfuric acid solution.

Table III
The $H_{0}$ Function in $20 \%$ Ethanol- $80 \%$ Aqueous Sulfuric Acid, and in Water

| N <br> $\mathrm{H}_{2} \mathrm{SO}_{4}$ | $-\mathrm{H}_{0}$ <br> $\mathrm{EtOH})^{a}$ | $-\mathrm{H}_{0}$ <br> $\left(\mathrm{H}_{2} \mathrm{O}\right)_{b}$ | N <br> $\mathrm{H}_{2} \mathrm{SO}_{4}$ | $-\mathrm{H}_{0}$ <br> $\mathrm{EtOH})^{a}$ | $-\mathrm{H}_{0}$ <br> $\left(\mathrm{H}_{2} \mathrm{O}\right)^{b}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 0.20 | -1.30 | -0.83 | 9.0 | 2.39 | 2.06 |
| 0.50 | -0.72 | -.44 | 10.0 | 2.82 | 2.28 |
| 1.00 | -.41 | -.13 | 11.0 | 3.24 | 2.51 |
| 1.50 | -.18 | +.07 | 12.0 | 3.65 | 2.76 |
| 2.00 | +.02 | .26 | 13.0 | 4.08 | 3.03 |
| 3.0 | .35 | .56 | 14.0 | 4.54 | 3.32 |
| 4.0 | .61 | .84 | 15.0 | 4.98 | 3.60 |
| 5.0 | .89 | 1.12 | 16.0 | 5.49 | 3.87 |
| 6.0 | 1.24 | 1.38 | 17.0 | 5.97 | 4.14 |
| 7.0 | 1.57 | 1.62 | 18.0 | 6.44 | 4.40 |
| 8.0 | 1.96 | 1.85 | 19.0 | 6.91 | 4.65 |
| $a$ Interpolated from the smoothed curve | $b$ Ref. 3. |  |  |  |  |

Some similarities and differences between the $H_{0}$ function in the two solvent systems are apparent from Fig. 2. In the range of low $\mathrm{H}_{2} \mathrm{SO}_{4}$ concentration $H_{0}$ values for $20 \%$ ethanolic $\mathrm{H}_{2} \mathrm{SO}_{4}$ are only slightly more positive than $H_{0}$ values for aqueous $\mathrm{H}_{2} \mathrm{SO}_{4}$. This is reasonable because, according to the definition, for dilute $\mathrm{H}_{2} \mathrm{SO}_{4}$ solutions, $H_{0}$ values in both solvents must be identical with the $p \mathrm{H}$ and it is known that the addition of ethanol to dilute $\mathrm{H}_{2} \mathrm{SO}_{4}$ solution at fixed $\mathrm{H}_{2} \mathrm{SO}_{4}$ content decreases the activity of hydrogen ion. A similar observation has been reported by Braude. ${ }^{4}$ Further, the $H_{0}$ function in both solvent systems increases almost linearly with the normality of the acid at higher acid concentrations ( $>5 N \mathrm{H}_{2} \mathrm{SO}_{4}$ ).


Fig. 2.--The $H_{0}$ function in $\mathrm{H}_{2} \mathrm{O}$ and in $20 \%$ ethanol $v s$. sulfuric acid normality.

The most striking difference between the two solvent systems is that in 20 vol. \% ethanolic $\mathrm{H}_{2} \mathrm{SO}_{4}$ $H_{0}$ increases much more rapidly than in aqueous solution at $\mathrm{H}_{2} \mathrm{SO}_{4}$ concentrations above $5 \mathrm{~N}^{15,16}$ The apparently greater acidity of the ethanolic $\mathrm{H}_{2} \mathrm{SO}_{4}$ solutions compared with the aqueous solutions at a fixed $\mathrm{H}_{2} \mathrm{SO}_{4}$ concentration above 5 N can be explained by a consideration of the relative basicities of water and ethanol. It has been shown that water is a stronger base than ethanol, i.e., the conjugate acid of ethanol is a stronger acid than the conjugate acid of $\mathrm{H}_{2} \mathrm{O}$, and the equilibrium

|  |  | Table IV |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $p K^{\prime} s$ |  |  | $\mathrm{Y}^{\text {IN } 20}$ | $\mathrm{EtOH}$ |
|  | $\mathrm{Y}-\mathrm{NO}$ m | $\mathrm{Y}=\mathrm{H}$ |  | $\stackrel{\mathrm{Y}-\mathrm{OH}}{\mathrm{O}}$ |
| x | - $p \mathrm{~K}$ | $-p K$ | - 2 K | $\rightarrow->K$ |
| 4-OF.t | $2.48 \pm 0.03$ | $1.28 \pm 0.02$ |  |  |
| 4 -OMe | $2.54 \pm .03$ | $1.36 \pm .03$ | $0.75 \pm 0.03$ | $0.56 \pm 0.03$ |
| 4-Me | $3.83 \pm .02$ | $2.35 \pm .02$ | $1.03 \pm .02$ | $0.84 \pm .03$ |
| 3-Me | $4.32 \pm .02$ | $2.70 \pm .03$ |  |  |
| H | $4.63 \pm .02$ | $2.90 \pm .02$ | $1.36 \pm .03$ | $1.02 \pm .01$ |
| ${ }_{4}-\mathrm{Br}$ | $5.04 \pm .01$ | $3.47 \pm .02$ | $1.74 \pm .03$ | $1.42 \pm .01$ |
| $3-\mathrm{Br}$ | $5.52 \pm .02$ | $3.83 \pm .03$ | $2.06 \pm .02$ | $1.67 \pm .01$ |
| $3-\mathrm{COCH}_{3}$ | $5.69 \pm .02$ |  |  |  |
| $4-\mathrm{COCH}_{3}$ | $5.96 \pm .02$ | $3.98 \pm .04$ | $2.23 \pm .02$ |  |
| $4-\mathrm{CN}$ | $6.50 \pm .04$ | $4.52 \pm .02$ |  |  |
| $3-\mathrm{NO}_{2}$ | $6.57 \pm .07$ | $4.63 \pm .02$ | $2.54 \pm .03$ |  |
| $4-\mathrm{NO}_{3}$ |  | $4.70 \pm .02$ |  |  |
| O-Nitro | niline, $p K=$ | -0.34; p-n | itroaniline, | $K=0.93$ |
| $\begin{aligned} & \text { (15) H. } \\ & \text { Braude, } J . \end{aligned}$ | oldschmidt, $Z$ hem. Soc.. 443 | physik. Chen (1944). | $n ., 89,129$ | 14) ; E. A. |

constant for the reaction

$$
\mathrm{EtOH}_{2}{ }^{+}+\mathrm{H}_{2} \mathrm{O} \rightleftarrows \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{EtOH}
$$

has been estimated to be the order of $1 \overline{0}$. Thus, when we compare solutions of $\mathrm{H}_{2} \mathrm{SO}_{4}$ in water and in $20 \%$ ethanol at fixed $\mathrm{H}_{2} \mathrm{SO}_{4}$ content, we expect that the latter solution has higher apparent acidity due to the presence of $\mathrm{EtOH}_{2}{ }^{+}$which is absent fronn the former. In other words, ethanol has a "leveling effect" to exhibit higher acidity. This phenomenon is also observed in the study of the $H_{0}$ function of a non-aqueous solvent system, e.g., acetic acid. ${ }^{17}$

Part of the steeper increase of $H_{0}$ for $20 \%$ ethanolic $\mathrm{H}_{2} \mathrm{SO}_{4}$ compared to aqueous $\mathrm{H}_{2} \mathrm{SO}_{4}$ may be attributed to the more rapid increase in the molar concentration of ethanol in the mixed solvent system at higher $\mathrm{H}_{2} \mathrm{SO}_{4}$ concentrations. The increment in mole per cent. ethanol per unit increase of $\mathrm{H}_{2} \mathrm{SO}_{4}$ concentration expressed in normality is 0.1 at $3 N$ to $6 \mathrm{NH}_{2} \mathrm{SO}_{4}, 0.3$ at $8 \mathrm{H}_{2} \mathrm{SO}_{4}, 0.38$ at $12 \mathrm{NH}_{2} \mathrm{SO}_{4}, 0.5$ at $16 \mathrm{NH}_{2} \mathrm{SO}_{4}$ and 0.65 at 19 N $\mathrm{H}_{2} \mathrm{SO}_{4}$, respectively.
It is interesting to note that, at the higher acid concentrations, the more rapid increase of $H_{0}$ in $20 \%$ ethanol compared with the aqueous solutions persist even when the acid concentration is plotted as mole fraction.

The $H_{0}$ function presented here offers several advantages. It is based on a series of very closely related indicators, all of which, with the exception of $o$ - and $p$-nitroaniline, are derivatives of azobenzene. They differ only in the nature of the substituents, which are reasonably far removed from the basic center. Hence it appeared reasonable that the activity coefficient ratio would remain reasonably constant throughout the series. That this expectation actually was realized appears to be borne out by an examination of Fig. 1, where it is seen that overlapping portions of the $\log (B /$ $\mathrm{BH}^{+}$) os. acid concentration plots are quite close to being parallel. Comparison with previous curves (cf., e.g., the plot given in Fig. 1 of ref. 3) indicates that in this respect the choice of the structurally closely related indicators had the desired effect.

These same results do, of course, raise the question again whether a truly general acidity function exists. Until indicators of different structure will have been investigated by this acidity function this question must remain unanswered.

A further advantage of the present $H_{0}$ function in $20 \%$ ethanolic $\mathrm{H}_{2} \mathrm{SO}_{4}$ lies in its usefulness for the measurements of $p K$ 's of weak, uncharged bases which are not very soluble in dilute aqueous acid. The particular solvent system chosen has the advantage that it facilitates the prepatation of a series of solutions of different $\mathrm{H}_{2} \mathrm{SO}_{4}$ concentrations but identical concentration of base and ethanol, and hence makes convenient the measurement of the concentration ratios by the spectrophotometric method.

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